

# CB VII

## Molecular Orbital (MO) Theory

Ref 11: 3

Prob FUP: 11: 3, 4  
E of C: 11: 32 – 37, 51

Adv Rdg 5: 1 - 5

## Basic Principles

Wave mechanical theory  
is applied to bonding in a molecule as a whole  
i.e., includes interaction of **all nuclei & e<sup>-</sup>s**

Schroedinger equ<sup>n</sup> is solved for allowed  
wave states, or wave functions,  $\Psi$ ,  
which, in turn, provide a description molecular  
orbitals (MO's)

as a result we get a set of discrete MO's  
describing energy & "location" of e<sup>-</sup>s

important to realize that MO's cover the molecule  
as a whole (e<sup>-</sup>s are "delocalized"),  
rather than being strictly located on or between  
individual atoms

## General

further improvement on Lewis, VSEPR & VB  
theory;

resulting in better info on:

bond energy  
bond order  
magnetic properties of molecules

.....

.....

## Basic Ideas

- problem very complex
- no exact solutions exist
- various approximations are applied,  
esp. LCAO method  
("linear combination of atomic orbitals")
- start off w/ AO's of bound atoms
- generally, combine AO's that are close in:
  - proximity,
  - orientation,
  - energy
 to form MO's

basic ideas ...

- use wavemechanical concepts, esp. aspects of wave interference (constructive and destructive) to construct MO's

- generally,  
# of MO's = # of "originating" AO's

half of MO's are lower in energy than the originating AO's = **bonding MO's**

half of MO's are higher in energy ...  
= **antibonding MO's**

basic ideas ...

- apply principles you know from AO Theory to fill a set MO's w/  $e^-$ 's as follows:

"Aufbau"

in ground state lowest energy MO's are occupied

"Pauli"

max. of 2  $e^-$ 's per MO;

if 2 are present, they have opposite spins

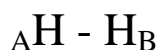
"Hund"

if MO's are degenerate,

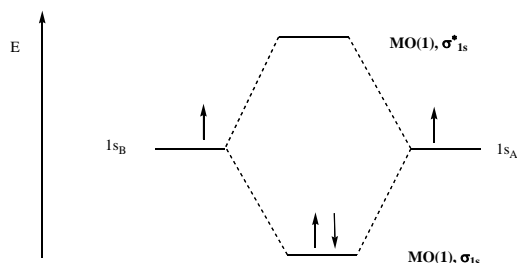
fill MO's singly first (w/ same spin)

before doubling up

## Application to H<sub>2</sub> Molecule



Energy Diagram



$$\text{MO}(1) = 1s_A + 1s_B$$

$$\text{MO}(2) = 1s_A - 1s_B$$

2  $e^-$ 's available,

only the bonding MO, σ<sub>1s</sub>, will be filled,

∴ H<sub>2</sub> stable !!

H<sub>2</sub> molecule ...

equivalent expression :

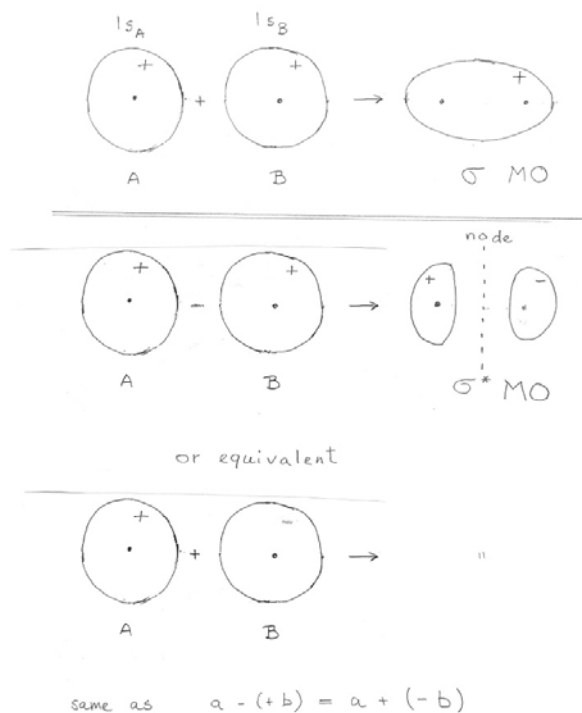
1s<sub>A</sub> & 1s<sub>B</sub> AO's combine

**in - phase** to form bonding MO's

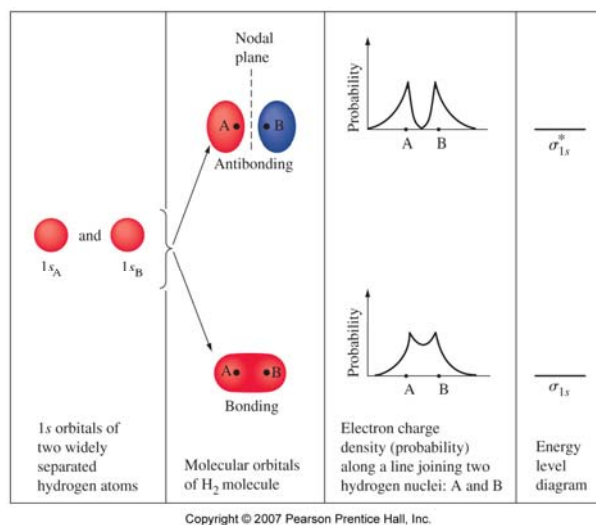
&

**out - of - phase** to form antibonding MO's

## Orbital Diagrams for H<sub>2</sub>



Pet. Fig.11.20 MO Theory for H<sub>2</sub>



## Bond Order by MO Theory

General:

$$\text{B.O.} = \frac{\text{bonding } e^{-}\text{'s} - \text{antibonding } e^{-}\text{'s}}{2}$$

for H<sub>2</sub>:

$$\text{B.O.} = \frac{2 - 0}{2} = 1 \quad (\text{single bond})$$

in this case, agrees w/ Lewis theory

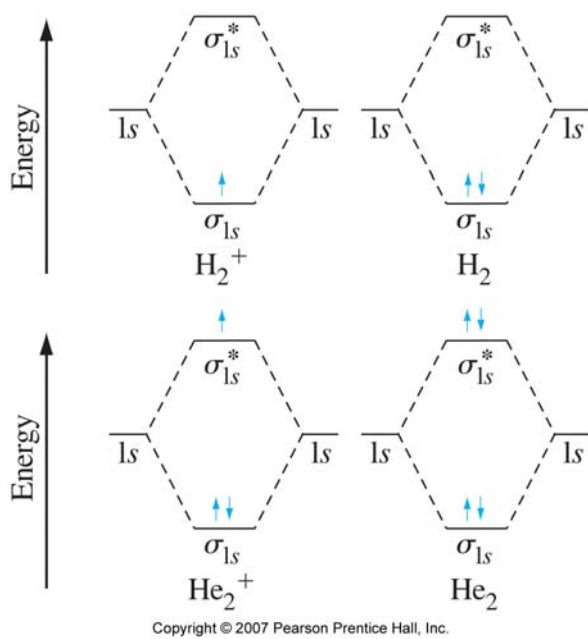
## Other Row 1 Species

see Pet. Fig. 11.21

evaluate for B.O. and stability:

species	B.O.	Existence
H <sub>2</sub> <sup>+</sup>	0.5	known
He <sub>2</sub> <sup>+</sup>	0.5	"expected"
He <sub>2</sub>	0	unknown, not expected

Pet. Fig. 11.21 MO diagrams for diatomic row 1 species



## MO Theory for Row 2 Molecules (diatomic, homonuclear)

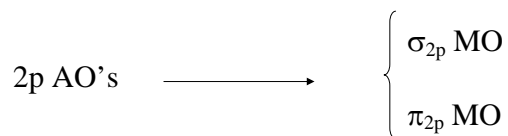
Generally,

can ignore core AO's ( i.e., 1s AO's)

(because weak interaction;  
also, bonding & antibonding MO's cancel)

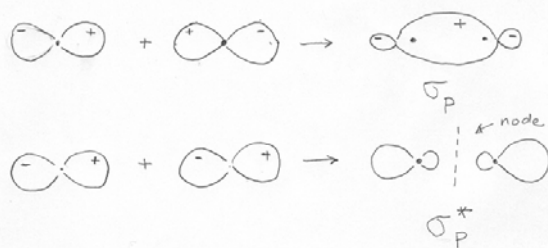
i.e., work w/ valence  $e^-$ 's

significant combinations in row 2 orbitals:

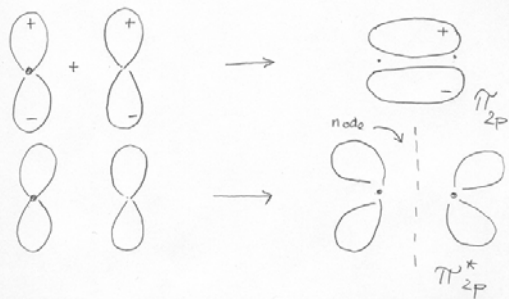


## Combination of p AO's

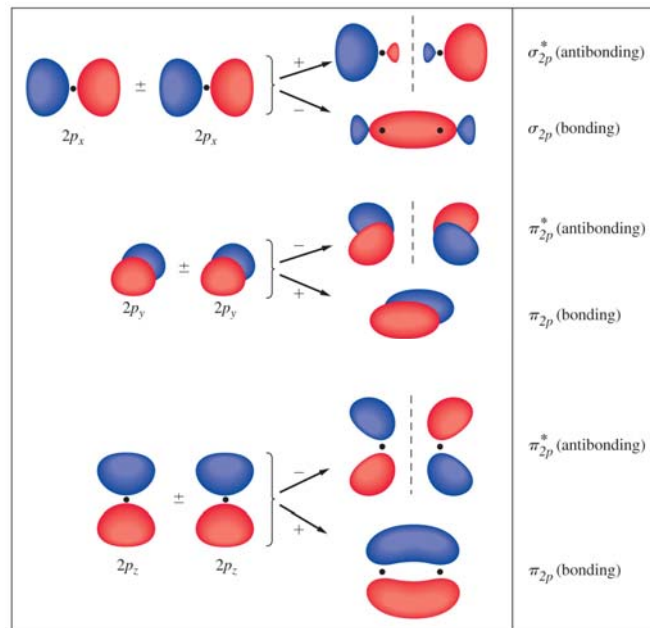
$\sigma$  style, "head-on"



$\pi$  style, "sideways"



Pet. Fig. 11.23 MO's from 2p AO's



# MO Energy Diagrams

$\sigma_{2s}$  lower than  $\sigma_{2p}$ ,  $\pi_{2p}$

(b/c originating 2s AO's are lower than 2p AO)

expect that  $\sigma_{2p}$  is lower than  $\pi_{2p}$

( $\sigma_{2p}$  has more overlap than  $\pi_{2p}$ )

“expected” MO diagram  
(HT Fig. 14.1)

but exceptions are common

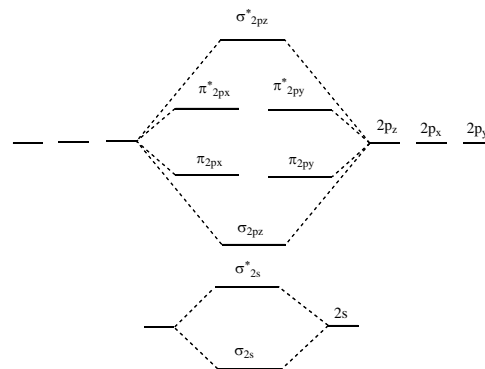
“modified” MO diagram  
(HT Fig. 14.2)

# General MO Energy Diagram

## Expected

valid for  $O_2$ ,  $F_2$ , ( $Ne_2$ )

HT Fig. 14.1

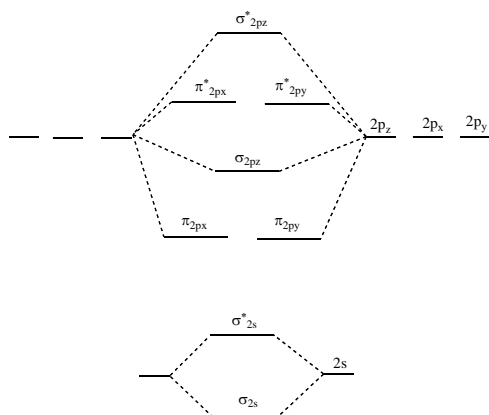


# General MO Energy Diagram

## Modified

valid for  $Li_2$  ....  $N_2$

HT Fig. 14.2



# Practice

Complete MO Energy Diagrams for

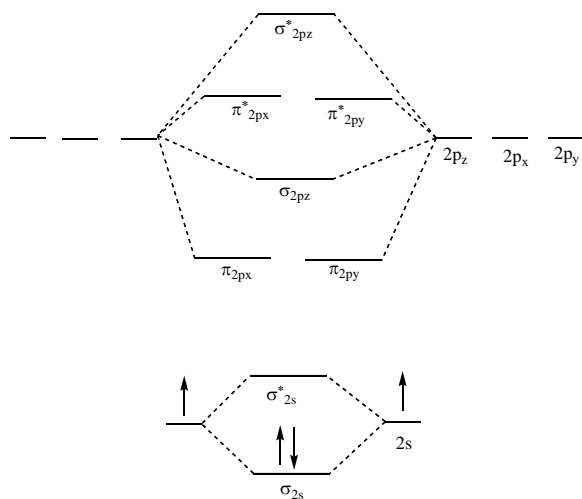
$Li_2$ ,  $B_2$ ,  $N_2$ ,  $O_2$

- fill MO diagrams w/  $e^-$ 's
- determine B.O.
- assess magnetism

For completeness sake, you may want to do

$Be_2$ ,  $C_2$ ,  $F_2$ ,  $Ne_2$  also

## MO Energy Diagram for $\text{Li}_2$

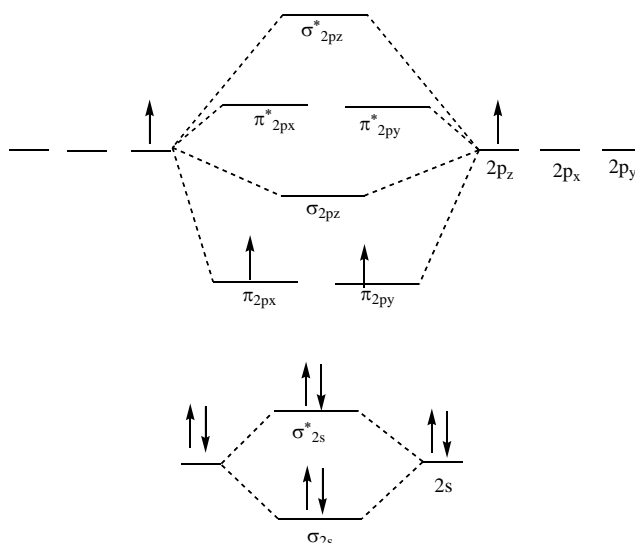


$$\text{B.O.} = \frac{2 - 0}{2} = 1$$

all  $e^-$ 's paired

$\therefore$  diamagnetic

## MO Energy Diagram for $\text{B}_2$

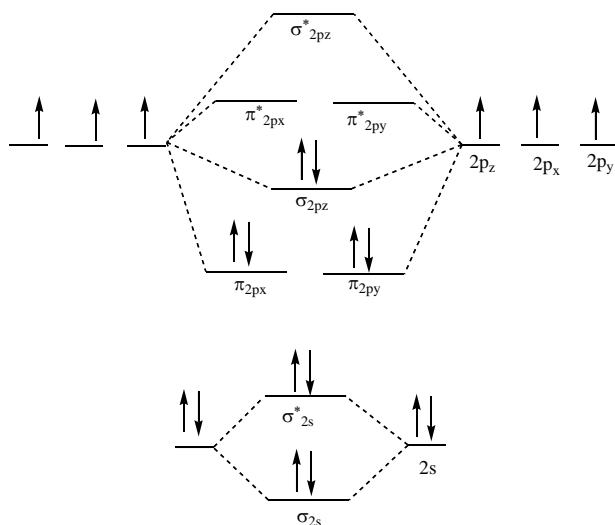


$$\text{B.O.} = \frac{4 - 2}{2} = 1$$

2  $e^-$ 's unpaired

$\therefore$  paramagnetic

## MO Energy Diagram for $\text{N}_2$

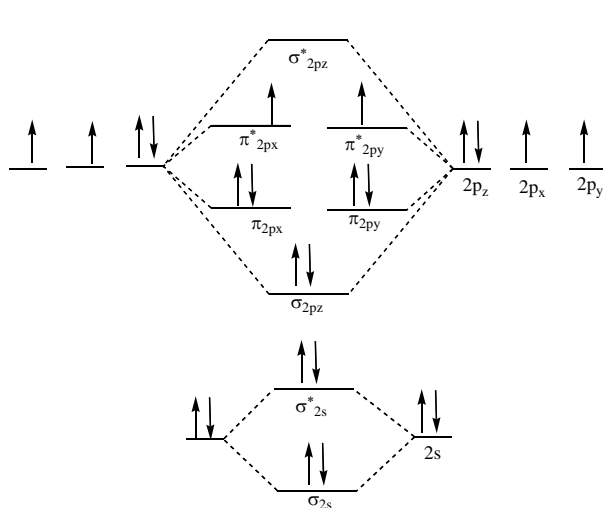


$$\text{B.O.} = \frac{8 - 2}{2} = 3$$

all  $e^-$ 's paired

$\therefore$  diamagnetic

## MO Energy Diagram for $\text{O}_2$



$$\text{B.O.} = \frac{8 - 4}{2} = 2$$

2  $e^-$ 's unpaired

$\therefore$  paramagnetic

## Summary

Pet. Fig. 11.25 provides a summary of MO's for all row 2 diatomic homonuclear molecules.

*Derive, don't memorize*

Pet.Fig. 11.23 Summary of MO theory for row 2 diatomics

$\sigma_{2p}^*$	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
$\pi_{2p}^*, \pi_{2p}^*$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2p}$	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\pi_{2p}, \pi_{2p}$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2s}^*$	<input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2s}$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
	Li <sub>2</sub>	Be <sub>2</sub>	B <sub>2</sub>	C <sub>2</sub>	N <sub>2</sub>
Bond order	1	0	1	2	3
Magnetism	Dia-magnetic	–	Para-magnetic	Dia-magnetic	Dia-magnetic

$\sigma_{2p}^*$	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\pi_{2p}^*, \pi_{2p}^*$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\pi_{2p}, \pi_{2p}$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2p}$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2s}^*$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
$\sigma_{2s}$	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>	<input type="checkbox"/> <input type="checkbox"/>
	O <sub>2</sub>	F <sub>2</sub>	Ne <sub>2</sub>
Bond order	2	1	0
Magnetism	Para-magnetic	Dia-magnetic	–

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## Comments

- Use the same diagrams to analyze (stability, B.O., magnetism ...) charged homonuclear species, such as N<sub>2</sub><sup>+</sup>, O<sub>2</sub><sup>–</sup>, etc.
- similar analysis applies to **row 3** diatomic molecules  
Na<sub>2</sub> ..... Ar<sub>2</sub>  
Combine 3s and 3p AO's to get  
 $\sigma_{3s}$ ,  $\sigma_{3p}$ ,  $\pi_{3p}$  MO's  
(again bonding & antibonding etc.)

## Heteronuclear Diatomics (e.g., CO, NO)

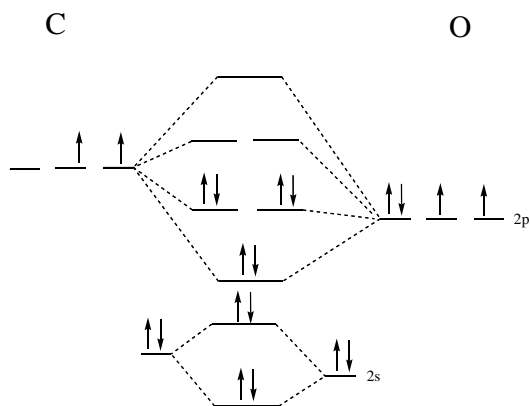
when molecule contains O

apply “**expected**” MO energy diagram,  
but in a “**distorted**” form

(originating AO's of more e/n atom are lower in energy, causing this distortion)

see CO as an example, HT Fig.14.3

## HT Fig. 14.3 MO Energy Diagram for CO



$$\text{B.O.} = \frac{6 - 0}{2} = 3$$

all  $e^-$ 's paired

$\therefore$  diamagnetic

## Overall Comment on Bonding

- MO theory generally gives best results, but often very complicated
- in many cases, simpler theories are satisfactory
- “practicing chemists” use a mixture of all theories, “whatever works best”
- e.g., in organic chem.:
  - for  $\sigma$  bonds: use VB theory, including hybridization of AO's
  - for  $\pi$  bonds: use MO theory, including resonance ideas from Lewis theory